

BHs and GWs: Leading frontiers in astrophysics

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Abstract:

This article introduces the black holes as one of the most important objects in the universe, the existence of BHs has an important impact on the generation of GWs. GWs are ripples caused by changes in the curvature of space-time, and their source is closely related to the accelerating motion of large celestial bodies. This paper discusses the role of GWs in the evolution and development of black holes, and analyzes the effects of black holes with different masses and spins on GW signals. By analyzing data captured by GW detectors, we have revealed how merger events between black holes provide important information about the nature of BHs and the evolution of the universe. In addition, the potential contribution of future development of detection techniques to deepening the understanding of the relationship between BHs and GWs is discussed. The results show that BHs are not only the source of GWs, but also an important window into the deep structure of the universe.

Keywords

1. Introduction

BH is a background of space-time which is that the gravity so strong that nothing, not even rays, can escape. GR thinks that sufficiently dense mass can warp spacetime to create black holes. The edge beyond which escape is impossible which thought like the event horizon. While a black hole significantly influences the fate and environment of nearby objects, general relativity indicates that it has no locally detectable features. In many respects, a black hole behaves like an ideal black body, as it does not reflect light. Quantum field theory thinks that the Event horizon emits Hawking radiation, which has the same spectrum as a black body, with a temperature inversely proportional to its mass. For a stellar black

hole, this temperature is around one billionth of a Kelvin, making direct observation nearly impossible. GWs are transient perturbations in the gravitational field, produced by the motion or acceleration of gravitational mass, propagating outward from the source at the speed of light. Oliver Heaviside proposed that in 1893 and further Henri Poincare developed that in 1905, considering them as gravitational analogies for electromagnetic waves. In 1916, Albert Einstein proved that GWs are ripples in space-time described by his theory of general relativity.

Black holes may be the most interesting objects in the universe. They distort the space-time around them, preventing all matter, including light, from escaping. They come in different sizes, or better quality, and they can be quite elusive.

Intermediate-mass black holes have been predicted in theory, but so far only preliminary observational evidence exists, either as an ultra-bright X-ray source or as a spike in the density curve of a dense cluster of stars. Of particular interest is the possibility of black holes forming binary stars, which contract in separation until the two components collide and merge into a single black hole, releasing energy in the form of GWs. They can travel through the universe unaffected, just ripples in the fabric of spacetime.

The field of GW astronomy has been revolutionized by LIGO's discovery of GWs from compact binaries [1]. Recognition of random background by pulsar timing array. These breakthrough discoveries not only open new Windows in astrophysics and cosmology, but also raise many profound questions. From revealing the astrophysical origins of compact inspiration systems and their applications in measuring the expansion rate of the universe, to exploring the bizarre realm of primordial black holes, the spectrum of research is vast and vibrant.

In addition, the random background of GWs hints at mergers of supermassive black holes and may provide constraints on remnants of phenomena in the early universe, providing a unique perspective to explore the origin of supermassive black holes and their role in galaxy evolution [2].

2. Theoretical framework

2.1 Black holes

When a star more than eight times the mass of the Sun runs out of fuel, its core collapses, rebounds, and then explodes as a supernova. The material left behind depends on the mass of the star before it exploded. If it approaches the critical value, it will form a city-sized, super-dense neutron star. If it is 20 times the mass of the Sun or more, the core of the star will collapse into a stellar-mass black hole.

To date, nearly all observed Stellar-M BHs which have been identified due to their association with companion stars. These black holes often form from binary star systems, where the more massive star rapidly evolves into a black hole. In certain cases, referred to as X-ray binaries, the black hole siphons gas from its companion star, creating an accretion disk heated enough to emit X-rays. Within the Milky Way, approximately 50 suspected or confirmed Stellar-M BHs have been detected, but estimates suggest there could be as many as 100 million of them in our galaxy [3].

In addition to stellar-mass black holes, almost every large galaxy, including our MW, hosts a Super-m BH at its

center. These colossal entities can range from hundreds of thousands to billions of times the mass of the Sun, with some scientists suggesting a minimum mass of tens of thousands of solar masses. Observations of distant galaxies indicate that some Super-M BHs may have formed within the first billion years after the universe's inception, possibly arising from the collapse of Super-M stars in the early universe.

Despite the uncertainties surrounding their origins, it is understood that supermassive black holes can grow by accreting smaller objects, including stellar-mass black holes and neutron stars. They can also merge with other supermassive black holes during galactic collisions, further contributing to their growth[3].

Researchers have long pondered the size between Stellar M and Super M black holes. They theorize that there should be a continuum of mass and volume, as collisions between Stellar-M BHs over cosmic time could lead to the formation of Intermediate-M BHs. These intermediate-mass black holes would typically range from about 100 times to several hundred thousand times the mass of the Sun, depending on how one defines a Super-M BH[3].

2.2 GWs

General relativity is a theory of gravity proposed by Albert Einstein in 1915, serving as the current framework for understanding gravity in modern physics. It generalizes special relativity and enhances Newton's law of universal gravitation, portraying gravity as a geometric property of spacetime.

GR suggests that gravity has a velocity, the same as the velocity of light rays. Large disastrous events, such as collisions between BHs or neutron stars, produce GWs [4].

3. Observational techniques

3.1 Detecting BHs

A BH is detected when surrounding matter, such as gas, flows into a disk around it under the pull of gravity. The gas molecules in the disk are spinning around the BH so fast that they are heated and give off X-rays. These X-rays can be detected from Earth.

Gravitational lensing can help identify isolated BHs that would otherwise be invisible, as these massive objects bend and distort the light from more distant sources.

This array connects eight existing radio observatories on Earth to create a virtual telescope the size of the Earth. Using the Event Horizon Telescope (EHT), astronomers can observe the plasma ejected by BHs, detect ripples in spacetime caused by BH collisions, and may soon visual-

ize the disrupted disk of mass and energy surrounding a BH's event horizon, from which nothing can escape.

3.2 Detecting GWs

LIGO is that the Laser Interferometer Gravitational-Wave Observatory. It comprises two large laser interferometers located 3,000 kilometers apart, utilizing the principles of light and spacetime to detect and analyze the origins of GWs.

The Virgo interferometer is a big facility specifically designed to detect the GWs predicted by general relativity.

4. Recent Discoveries

Logic analysis, the quality of these massive BHs, each hole is billions of times the Sun, will inevitably experience collisions and mergers. This merging process can pull much more of material into the BH, causing violent astrophysical explosions that can affect star formation and other related processes in the host galaxy. So far, however, astronomers have only observed flashes at certain moments in this long process, which begins when the BHs are separated by hundreds of light years. As the merging BHs shrink in distance, it becomes harder to tell them apart.

In a new study which is published by *Astrophysical Journal Letters*, an international team of scientists announced the discovery of two active Super-M BHs near Earth. According to the calculation, the two BHs respectively with the quality of the 125 million times and 200 million times the sun, about 5 light years, they are consuming UGC 4211 center, everything around the UGC 4211 is a state is still in the merger of the galaxy. "These objects are very exciting because they are very close to each other and very close to us," said one of the study's authors, Chiara Mingarelli, an astrophysicist at the Iron Iron Institute in New York City and the University of Connecticut. The distance between the two is only 750 light-years, equivalent to 230 parsecs, which is confirmed by measuring the spectrum of multiple wavelengths, and is the closest known pair of BHs to date. This discovery not only provides a unique opportunity for fundamental research on large BH mergers, but also provides a good opportunity to detect one of their most elusive - ripples in space-time, known as GWs.

The two BHs in UGC 4211 are considered to be in the consolidation stage. As the cosmic twins develop, they will come closer and closer as a cluster of stars and gas around them suck up orbital momentum. The authors predict that this dance will end in about 200 million years, when the two supermassive BHs will finally fully merge into one[5].

The payoff should be worthwhile: Such huge mergers are seen as one of the main contributors to the "GW background". The "GW background" refers to the sum of ripples in space-time created by sources that have not yet been detected but exist throughout the observable universe, leaving an imprint on the sky. Mingarelli points out that detecting and mapping this background will reveal "the merger history of the supermassive BH universe" and a lot of other important cosmological information. Delving into the details of merging systems like UGC 4211 could help researchers better understand what they're observing and, ultimately, the background of GWs in the universe[6].

When two initially unbound BHs gradually approach each other, their trajectories can transition to bound orbits through the emission of GWs during encounters within a star gatherings. This phenomenon illustrates one aspect of the relationship between GWs and BHs, commonly referred to as GW capture.

Since LIGO's first detection of GWs in 2015, several BH binaries and one neutron star binary have been identified during LIGO and Virgo's initial observation periods. BH binaries can form through various dynamical processes, including three-body interactions, GW-driven capture, and the evolutionary processes of stellar binaries. A important counts of these binaries are likely to form in the dense environments of star clusters, such as globular clusters or nuclear star clusters within galaxies.

GW capture, happens when unbound BHs come close together and lose orbital energy by emitting GWs. This process is typically thought to be more effective in galactic nuclei than in globular clusters, primarily due to the higher density of BHs necessary for effective capture. However, recent studies that incorporate post-Newtonian dynamics suggest that GW capture can also occur frequently within globular clusters, especially during chaotic interactions involving binary-single or binary-binary systems.

GW capture an interesting result is which can be produced very eccentric small binary, they can merge with significant eccentric. Some BH binary stars formed by GW capture do not have enough time to cycle by emitting GW before merging. When they pass through the current interference GW detectors band, they can have significant eccentric, even they merge. Thus, their GWs can be different from those of the circuit. Depending on the orbit, they can have waveforms modulated due to eccentric or repetitive burst-like waveforms.

In addition to the traditional astrophysical BHs at the center of a cluster where GW (GW) capture occurs, some research suggests that primordial BHs may also engage in GW capture. BHs with masses ranging from 20 to 100 M_{\odot} represent a potential avenue for understanding dark

matter. Primordial BHs within this mass range could constitute a component of dark matter, and close encounters between them might lead to gravitationally bound states through the emission of GWs.

In addition to the GW capture involving traditional astrophysical BHs at the center of a cluster, some studies propose that GW capture may also occur between primordial BHs. BHs with masses ranging from 20 to 100 M_{\odot} remain viable candidates for dark matter, suggesting that primordial BHs in this range could contribute to dark matter. Close encounters between these BHs may result in gravitationally bound states through the emission of GWs.

In before's and now, we focused on GWC during very close encounters. While several studies have explored GW capture and the properties of hyperbolic orbits using post-Newtonian (PN) calculations, close encounters and mergers necessitate a full general relativistic approach. We conducted numerical relativity (NR) simulations and compared the results with PN predictions. Previous studies have examined GW capture in full general relativity for equal-mass BHs. The critical impact parameter $b(\text{crit})$ for marginal capture depends on the relative velocity at infinity $v(\infty)$, following the relation $b(\text{crit}) \propto v(\infty)^{-9/7}$ in weak encounters, as derived from 2.5 PN calculations. However, in strong collisions characterized by shorter interaction times and relatively high speeds, $b(\text{crit})$ deviates from PN results and increases. This PN deviation is particularly pronounced in high mass ratio collisions, indicating that PN calculations for GW capture should be approached with caution in such scenarios.

No consideration of BHs spin in paper 1, but it is well known that spin can affect the orbit and GW radiation. Many studies, including Campanelli et al. (2006), have reported that the spin direction of a quasicircular orbit causes the change of a BH's orbit. In this study, we studied the BH spin by NR simulation of GW radiation and capture the GW impact parameters [7].

5. Analytical data

The emission of radiation from supermassive BHs results from the process of accretion, where gas spirals inward from a significant distance. As this gas descends into the BH's gravitational well, some of the released potential energy is transformed into thermal energy, which ultimately radiates as light. A crucial concept in this context is the Eddington threshold, which defines the maximum brightness of a gravitating entity. At this threshold, the outward force of radiation pressure is counterbalanced by the inward pull of gravity.:

$$L_E = \frac{4\pi GMm_p c}{\sigma_T} = 1.25 \times 10^{38} \frac{M}{M_{\odot}} \text{ erg s}^{-1}, \quad (1)$$

In this context, M represents the mass of the object, where $M = 1.99 \times 10^{33} \text{ g}$ is the mass of the Sun, m_p denotes the mass of a proton, and $T = 6.65 \times 10^{-25} \text{ cm}^2$ similar with Thomson cross-section for electron scattering. A spherical entity in equilibrium cannot possess a luminosity L exceeding the Eddington luminosity L_E . Given that bright quasars typically exhibit luminosities around $L \approx 10^{46} \text{ erg s}^{-1}$, they must be extremely massive: $M > 10^8 M_{\odot}$. However, a large mass alone does not confirm that an object is a BH; size is also a critical factor. Observations of quasars and other active galactic nuclei (AGN) suggest that their dimensions are not significantly larger than the gravitational radius of a BH with mass M :

$$R_g = \frac{GM}{c^2} = 1.48 \times 10^5 \frac{M}{M_{\odot}} \text{ cm}. \quad (2)$$

Quasars small volume of the earliest signs from the fact that the quasars in a few days time scale apparent change. Since an object cannot vary substantially on timescales shorter than its light-crossing time, quasars are inferred to be no more than a light-day in diameter, that is, they must be less than $10^2 R_g$ in size. Modern restrictions are stricter. Quasars RXJ 11311231, for example, the gravitational microlensing observations showed that the X-ray emission from a size of $\sim 10 \text{ rg}$ area. Stricter and more direct limits are obtained from the K-line observation of iron (< Several R_g), which indicates that the gas orbits the central object at a fraction of the speed of light. Meet the quality and size limit is the only plausible on astrophysical objects of a supermassive BH [8].

Millions of stellar-mass BHs are believed to exist in our Milky Way galaxy and in every other galaxy in the universe; however, only 24 of these have been confirmed through dynamical observations.

These 24, whose masses are in the range $M = 5 \sim 30 M_{\odot}$, are located in X-ray binary systems. X ray is by the companion star is toward the BH accretion disk release of gases. Near the BH (radius 10 rg), accretion gas to the typical temperature of 107 K and x ray.

24 BH binaries naturally divided into two categories: (I) five continuous X-ray source, a BH is by their massive companion blowing wind power. (ii) The remaining 19 binaries are transient sources whose X-ray brightness varies greatly, from roughly Eddington brightness L_E to as low as $10^{-8} L_E$. A typical active transient BH for about a year, and then keep the decades of stationary state [8].

Whether there is a medium quality BH, namely quality is too big ($M \gg 100 M$) rather than by ordinary star for-

mation, but not in the galaxy's core of a BH? Such objects are known as medium quality BHs (IMBHs), it represents a new, unique category a BH. The leading candidate for the IMBH is the brightest ultra-bright X-ray source in the outer galaxy, with an observed luminosity that can reach 100-1000 times the Eddington luminosity of a 10-m BH. Although there are some promising candidate, but because of difficult to get quality dynamic measurement, not a confirmed [8].

6. Results

6.1 Insights Into BHs Dynamics

GWs are produced by two BHs orbiting each other, which eventually collide and merge into a new BH. During this merging process, these BHs experience a brief period of instability, accompanied by some fluctuations. GWs (GWs) are emitted throughout this series of stages.

After decades of rigorous research, scientists have conducted in-depth theoretical predictions of this process, all based on the fundamental principles of Einstein's theory. These predictions provide crucial insights for translating the detected patterns of GWs into an understanding of their origins.

The study of the final stages of binary star mergers primarily relies on perturbation theory, which offers a powerful tool for revealing the dynamics of complex GW sources.

In general relativity, an isolated BH in equilibrium is a straightforward object, described by just a few parameters: its mass, angular momentum, and charge. However, this simplicity is often absent in realistic scenarios due to the complex dynamics involved in gravitational collapse during BH formation. Active galactic nuclei, accretion disks, strong magnetic fields, and surrounding stars or planets introduce additional complications.

As a result, the dynamic evolution of BHs cannot be fully characterized by basic parameters alone and may remain perpetually in a state of perturbation. Due to these technical and conceptual challenges, approximations are frequently necessary to produce physically meaningful predictions. In many cases, researchers focus on BH spacetime described by a stable background with minimal perturbations. This approximation relies on perturbation theory, which is applicable when the gravitational field is primarily influenced by known solutions of Einstein's equations. Perturbation theory allows for the inclusion of additional sources, provided they are weak enough to produce only minor corrections to the overall geometry[9].

6.2 GW Implications

According to general relativity, quality object of time-space has "twisted" effect, the space-time is four dimensional space and time, Einstein used it to describe his early special theory of relativity.

These affect material through time and space curve, so that the earth moves round the sun cause the space-time curvature rotating, the moon around the earth's mass caused by the "dent" rotate, but the sun itself around the supermassive BH at the center of the Milky Way galaxy Sagittarius A * space caused by the large curvature rotating.

The development of GW technology has opened new avenues for the study of celestial bodies such as BHs and neutron stars. By detecting GWs, scientists can gain a more comprehensive understanding of the characteristics of these objects, including their mass, spin, and shape, thereby deepening our knowledge of them. Furthermore, the detection of GWs provides innovative experimental methods for the physical research of BHs and neutron stars, advancing the field as a whole

7. Discussion

The discovery of GWs has not only confirmed a significant prediction of Einstein's general theory of relativity but has also introduced a novel observational method for investigating extreme celestial objects such as BHs and neutron stars. By detecting these waves, scientists can achieve a deeper understanding of the characteristics of these entities, including their mass, spin, and morphology, thereby enhancing our comprehension of their fundamental nature. Furthermore, the observation of GWs provides new concepts and technical approaches for precision measurement technology, further advancing research in both physics and astronomy.

GWs are fundamentally distinct from traditional electromagnetic radiation, cosmic rays, and neutrinos which are the new marking point in astrophysics. They offer unprecedented insights into the processes and mechanisms underlying the formation and evolution of the universe and its celestial bodies. The direct detection of GWs—particularly through facilities such as the Laser Interferometer Gravitational-Wave Observatory (LIGO)—has opened an unparalleled portal for astronomical observations and marked a significant advancement in this field.

The discovery of GWs not only validates Einstein's theories but also highlights phenomena within the universe that elude conventional electromagnetic observation methods. By observing these waves, scientists can detect extreme astrophysical events such as BH collisions and neu-

tron star mergers, providing an extraordinary perspective on the formation and evolution of our universe. Thus, this discovery represents not merely an affirmation of existing theories but also a substantial expansion and refinement of our understanding of cosmic dynamics.

In addressing the BH information paradox, now have proposed a “holographic duality” theory that correlates lower-dimensional quantum systems with higher-dimensional gravitational theories. Inspired by this theory, scientists in fields such as condensed matter physics, nuclear physics, cold atom physics, and quantum computing have initiated new calculations and experiments to reinterpret the challenges they encounter in their respective domains. This interdisciplinary research reveals a more profound connection between quantum information and the geometry of spacetime, which, in turn, has enhanced BH physicists’ understanding of BH entropy.

The theoretical limitations of BH research mainly come from our understanding and application of the laws of physics, like the limits on the diameter of BHs, although there should be a limit on stellar BHs, because the size of stars is limited, but the diameter limits of primordial BHs (BHs that theoretically existed in the early days of the Big Bang) are not clear. In addition, while there are theoretical upper limits for the minimum BH mass (about 3 solar masses) and maximum BH mass, these theoretical limits need to be verified by further observations and studies.

In terms of observations, although technological advances have allowed us to observe more distant and smaller celestial phenomena, direct imaging of BHs remains a challenge. The BH’s strong gravitational field and the accretion disk of surrounding matter can obscure the BH itself, making direct observations difficult. In addition, due to the extreme physical conditions of BHs, the detailed structure of BHs cannot be directly observed by existing detection techniques.

Mainstream GW detectors mainly rely on detecting the tiny stretching and compression of GWs on space to achieve, but due to the limitations of current technology, can only detect larger GW events, and the detection of small-scale events is limited. This can result in missing important physical phenomena such as the early stages of GW bursts or low-energy GW events.

Since the main theoretical source of GWs is general relativity, we need to test the non-general relativistic polarization through the pulsar timing array, which can further verify and limit different gravitational theoretical models. The advantage of this approach is the ability to translate model-independent constraints into constraints on concrete models, thus testing the predictions of the theory more precisely.

8. Summary

8.1 Summary of findings

Supermassive BHs are closely related to the formation and evolution of galaxies. Many studies have shown that the mass of a galaxy’s central BH is correlated with the mass and luminosity of its host galaxy, and that the formation process of these supermassive BHs, which usually exist in the galactic center, is closely related to the evolution of the galaxy. Observations of BHs, especially images of BHs with the Event Horizon Telescope (EHT), have allowed general relativity to be validated under extreme gravitational fields.

GWs are perturbations in space-time produced by accelerating mass, predicted by general relativity. In 2015, LIGO successfully detected GWs for the first time, giving birth to GW astronomy. GWs give us information about extreme cosmic events such as BH mergers and neutron star mergers, telling us about their frequency, mass distribution and evolutionary history. GWs also provide clues to the early stages of the universe. Like the relationship between the cosmic microwave background radiation and the GW background may shed light on the nature and mechanisms of the early expansion of the universe. Through the study of GWs, we can better understand the Big Bang theory and the origin of the universe.

As two BHs, or more than one BH, come closer together, the GWs they interweave will merge with each other and produce the phenomenon of GW capture, which depends on the explanation of the relationship between GWs and BHs.

By analyzing the GW signal, the mass and spin of the merging BHs can be deduced. This information is crucial for understanding the mechanism of BH formation (e.g. through supernova explosions, stellar evolution, etc.) and the distribution of BHs in the universe.

The frequencies and wave-forms of GWs can help scientists distinguish between different types of BHs, such as ordinary BHs, supermassive BHs, and so on. These classifications help us understand the evolutionary history of BHs in the universe.

References

- [1] <https://www.surrey.ac.uk/astrophysics-research-group/research/black-holes>
- [2] M. Bailes, B. K. Berger, P. R. Brady, M. Branchesi, K. Danzmann. Gravitational-wave physics and astronomy in the 2020s and 2030s. 2021: 1-16
- [3] Daniel Baumann. Research : GWs. LecosPA. 2024: 1-3
- [4] Alberto Accomazzi. Einstein’s Theory of Gravitation waves.

Center for Astrophysics Harvard.2024: 1-4

[5] Nelson Christensen. Stochastic GW Backgrounds. 2018

[6] Allison Parshall. Colliding Supermassive BHs Discovered in Nearby Galaxy. 2023: 1-15

[7] Yeong-Bok Bae, Hyung Mok Lee, Gungwon Kang. GW

Capture in Spinning BH Encounters. 2020: 1-15

[8] Ramesh Narayan and Jeffrey E. McClintock. Observational Evidence for BHs. 2014: 1-13

[9] Kyriakos Destounis. Dynamical behavior of black-hole spacetimes. 2019: 1-10